

# Spending Allocation under Nominal Uncertainty: A Model of Effective Price Rigidity

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## THE PAPER IN A NUTSHELL

- ★ Countercyclical markups in aggregate key to get  $\pi \uparrow$  and  $c \uparrow$

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...with fixed (but **increasing with Hs' unc.**) firm-level markups.

## RELATED LITERATURE

- ▶ **Consumers' search in GE:** Coibion, Gorodnichenko, and Hong (AER, 2015); Kaplan and Menzio (JPE, 2016)
  - Them: real determinants (unemployment) of search cost;
  - Us: real search cost are fixed, nominal shocks influence exp. payoffs;
- ▶ **Extensive margins:** Phelps and Winter (1970), Rotemberg and Woodford (1999), Paciello, Pozzi, and Trachter (IER, 2019), Michelacci, Paciello, Pozzi (2020)
  - No nominal uncertainty;
- ▶ **Learning from Prices (IO):** Fishman (QJE, 1996), Benabou and Gertner (REStud, 1993), Janssen and Shelegia (AER, 2015) - they do not look to the typical firm's problem in macro;
- ▶ **Learning from Prices - Uncertainty (Macro):** Lucas (AER, 1972), Amador and Weill (JPE, 2010), Gaballo (REStud, 2018), Chahrour and Gaballo (REStud, forth.) - Learning from competitive prices: no signaling power;
- ▶ **Households' uncertainty:** Angeletos and La' O (JPE, 2020); Farhi and Werning (AER, 2019); Gabaix (AER, 2020); McKay, Nakamura and Steinsson (AER, 2016) etc... + Mackowiak and Wiederholt (ReStud, 2015) - Non-neutrality relies anyway on firms' rigidity.

# OUTLINE

- ▶ Model
- ▶ Demand-Driven Business Cycles
  - ▶ Aggregate Counter-Cyclical Markup
  - ▶ Firm-level Markups: A-cyclical but Endogenous to Hs' Uncertainty
  - ▶ Welfare
- ▶ Empirics: a test of inflation-driven shopping reallocation
- ▶ Extensions
  - ▶ Households' vs Local Firms' Uncertainty
  - ▶ Targeted Communication
  - ▶ Local Varieties
  - ▶ Firms' Common Uncertainty (sticky prices)

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## ELEMENTS OF THE MODEL

- ▶ Two markets for goods: local (markups  $> 0$ ) and competitive (no markups)
- ▶ Hs exert shopping effort to buy in competitive markets
  - drive to distant locations (Walmart vs local Safeway)
  - search info about local markets on temporary sale
  - search info to arbitrage across shops for different varieties
  - behavioral/psychological, shopping habits
- ▶ Local productivity blurs the correlation of local prices with aggregate nominal shocks
- ▶ When deciding on shopping effort Hs forecast inflation with local prices
  - firms set prices without any friction

## MODEL: HOUSEHOLDS

Household  $i \in [0, 1]$  on island  $j \in [0, 1]$ :

$$E \left[ \sum_{\tau=t}^{\infty} \beta^{\tau-t} \left( \frac{c_{ij\tau}^{1-\frac{1}{\gamma}}}{1-\frac{1}{\gamma}} - \varphi l_{ij\tau} - \psi_{ij} s_{ijt} \right) \middle| \Omega_{i,j,t}^u \right] \quad (1)$$

with shopping effort cost  $\psi_{ij}$ , with  $s_{ijt} \in \{0, 1\}$ .

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where  $\psi_{ij}$  is distributed as in a generalized Pareto

$$G(\psi) = 1 - \kappa \left( 1 - \frac{\psi}{\Psi} \right)^{\frac{\lambda}{\gamma-1}},$$

with  $\kappa > 0$ ,  $\lambda > 0$ , and  $\Psi = \frac{\varphi^{\gamma-1}}{\gamma-1}$  with support

$$[\underline{\psi}, +\infty] \text{ with } \gamma \leq 1$$

$$[\underline{\psi}, \Psi + \underline{\psi}] \text{ with } \gamma > 1$$

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Shocks and prices

$P_t$  and  $p_{jt}$  realize

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Stage 1,

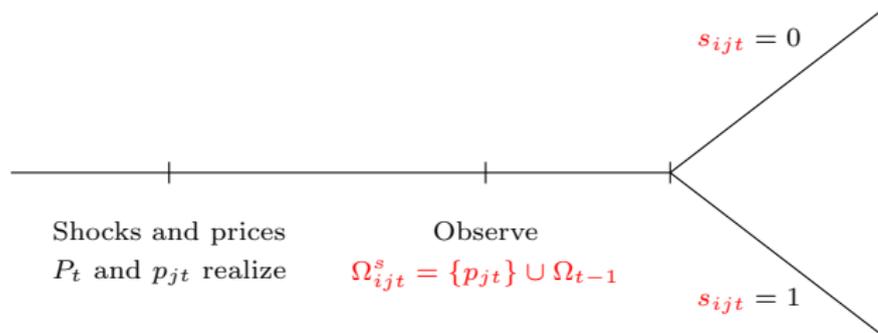


Shocks and prices  
 $P_t$  and  $p_{jt}$  realize

Observe  
 $\Omega_{ijt}^s = \{p_{jt}\} \cup \Omega_{t-1}$

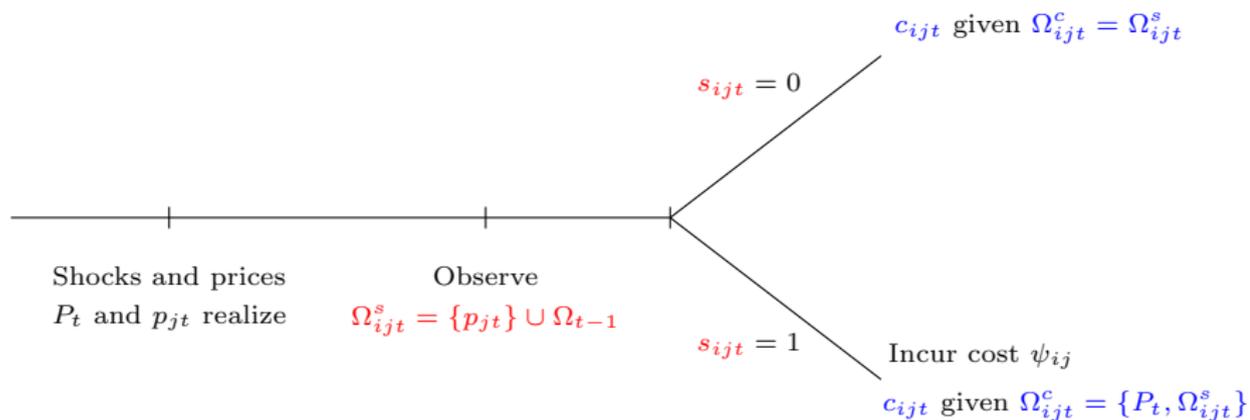
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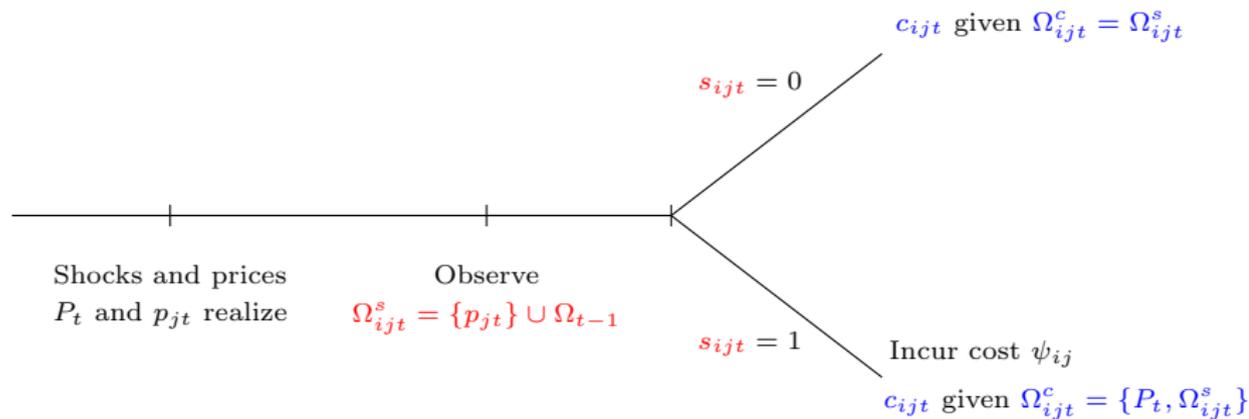
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Stage 1, Stage 2,



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Stage 1, Stage 2, Stage 3



$\{\ell_{ijt}, b_{ijt}\}$  in centralized markets  $\Rightarrow$  full info  $\Omega_t = \{P_t, \Omega_{t-1}\}$ .

## MODEL: FIRMS

- *Distant* competitive firms : linear technology in labor, thus

$$P_t = W_t \tag{3}$$

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$$P_t = W_t \quad (3)$$

- *Local heterogeneous monopolist* : maximize real profits under full info

$$\max_{p_{jt}} \left\{ \underbrace{\mathcal{N}(p_{jt}) \mathcal{C}(p_{jt})}_{D(p_{jt})} \left( \frac{p_{jt}}{W_t} - z_{jt} \right) \right\} \quad (4)$$

where :

- $\ln z_{jt} \sim N(z, \sigma_z)$  are i.i.d. productivity shocks
- $\mathcal{N}(p_{jt}) \subset (0, 1)$  is the mass of agents buying local
- $\mathcal{C}(p_{jt})$  denotes individual local consumption

## MODEL: AGGRGEATE SHOCKS AND MONETARY POLICY

- ▶ Aggregate shocks to:

$$\pi_t^w \equiv \ln W_t - E[\ln W_t | \Omega_{t-1}]$$

with  $\pi_t^w \sim N(0, \sigma_{\pi^w}^2)$ , where  $\pi_t^w = \pi_t$  from perf. competitive behavior.

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- ▶  $\Pi_t \equiv P_t/P_{t-1}$ , coinciding with wage inflation as given by (3).
- ▶ In particular, Monetary Policy implements the following AR(1) process

$$\ln \Pi_t = \chi \ln \Pi_{t-1} + \pi_t, \quad (5)$$

by appropriately setting  $R_t$  and  $T_t$ .

# EQUILIBRIUM DEFINITION

## DEFINITION

Given the past price level and inflation  $\{P_{t-1}, \Pi_{t-1}\}$  and a distribution of bond holdings  $\{b_{ijt-1}\}_{i,j \in [0,1] \times [0,1]}$ , the realizations of aggregate and idiosyncratic shocks,  $\pi_t$  and  $\{z_{jt}\}_{j \in [0,1]}$  respectively, a *log-normal equilibrium* is a collection of log-normally distributed prices  $\{P_t, W_t, R_t, \{p_{jt}\}_{j \in [0,1]}\}$ , and quantities  $\{s_{ijt}, c_{ijt}, b_{ijt}, \ell_{ijt}\}_{i,j \in [0,1] \times [0,1]}$  at time  $t$  such that:

- in each island  $j$ , each household  $i$  chooses  $\{s_{ijt}, c_{ijt}, b_{ijt}, \ell_{ijt}\}$  to maximize the expected utility (1) subject to the sequence of budget constraints in (2);
- $s_{ijt}$  and  $c_{ijt}$  are chosen first, according to the information sets  $\Omega_{ijt}^s$  and  $\Omega_{ijt}^c$  respectively,  $b_{ijt}$  and  $\ell_{ijt}$  are chosen at the end of the period under perfect information;
- in each island  $j$ ,  $p_{jt}$  solves the firm problem in (4);
- $W_t$  and  $P_t$  are determined, respectively, by equations (3) and (5);
- $R_t$  and  $T_t$  guarantee the equilibrium in the bond market, consistently with the monetary policy target in (5);
- $\int s_{ijt} di > 0$  holds almost surely in all islands.

**A non-trivial fixed point:** demand elasticity along extensive margins influence pricing, in turn pricing influences shopping choices by affecting Hs' expectations on  $p_{jt}/P_t$ .

## MARKETS OPEN SEQUENTIALLY. AT TIME $t$ , H CHOOSES:

STAGE 1  $s_{ijt} = 0$  iff:

$$E[V_{jt}(\psi_{ij}; 0) - V_{jt}(\psi_{ij}; 1) \mid \{p_{jt}\}] \geq 0.$$

i.e. iff  $\psi_{ij} > \hat{\psi}_{jt}$ , with  $\hat{\psi}_{jt}$  being an equilibrium object.

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STAGE 2 Consumption  $c_{ijt}$ :

$$c_{ijt}^{-\frac{1}{\gamma}} = \varphi E \left[ \frac{\mathcal{P}(s_{ijt})}{W_t} \mid \{\mathcal{P}(s_{ijt}), p_{jt}\} \right].$$

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STAGE 3 Labor  $\ell_{ijt}$  and Bonds  $b_{ijt}$ :

$$1 = \beta R_t E_t \left[ \frac{W_t}{W_{t+1}} \mid \{\mathcal{P}(s_{ijt}), p_{jt}, W_t, R_t\} \right].$$

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Shocks to  $R_t$  translates in shocks to

$$\pi_t^w \equiv \ln W_t - E[\ln W_t \mid \Omega_{t-1}]$$

where  $\pi_t^w \sim N(0, \sigma_{\pi^w}^2)$  represents a stochastic innovation to wage inflation.

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with  $\hat{\psi}_{jt} = \frac{\Psi}{\kappa} [1 - e^{(1-\gamma) (\ln p_{jt} - E[\ln P_t | \Omega_{jt}^s] + \frac{1}{2} \mathcal{S})}] \geq 0$  for any  $j$  almost surely;

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★ the consumption of household  $i$  initially matched to a island  $j$  is

$$c_{ijt} = \begin{cases} c_{jt}(p_{jt}) \equiv C^* e^{-\gamma (\ln p_{jt} - E[\ln W_t | \Omega_{jt}^s] + \frac{1}{2} \mathcal{S})} & \text{if } \psi_{ij} > \hat{\psi}_{jt} ; \\ C^* \equiv \varphi^{-\gamma} & \text{otherwise} \end{cases}$$

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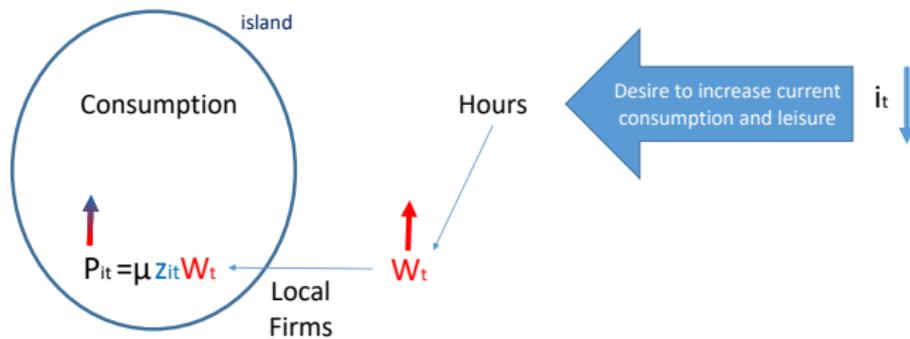
★ the optimal price posted by the monopolistic firm in island  $j$  is

$$p_{jt} = \underbrace{\frac{(\gamma + \lambda)(1 - \omega)}{(\gamma + \lambda)(1 - \omega) - 1}}_{\mu} \times \frac{W_t}{z_{jt}},$$

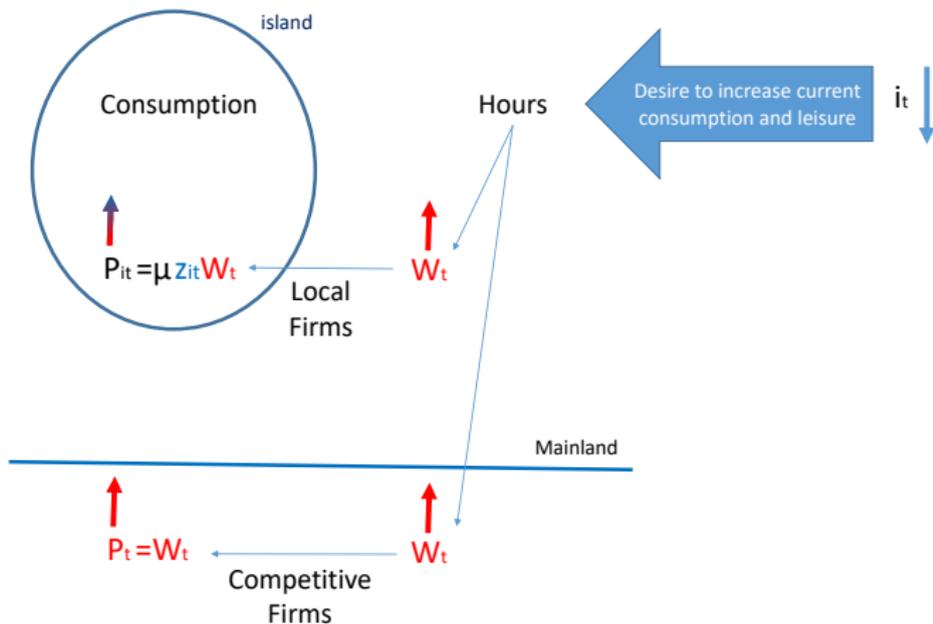
provided  $z$  is suff. large relative to  $\sigma_z$ , and  $(\gamma + \lambda)(1 - \omega) > 1$ .

## CARTOON SUMMARY

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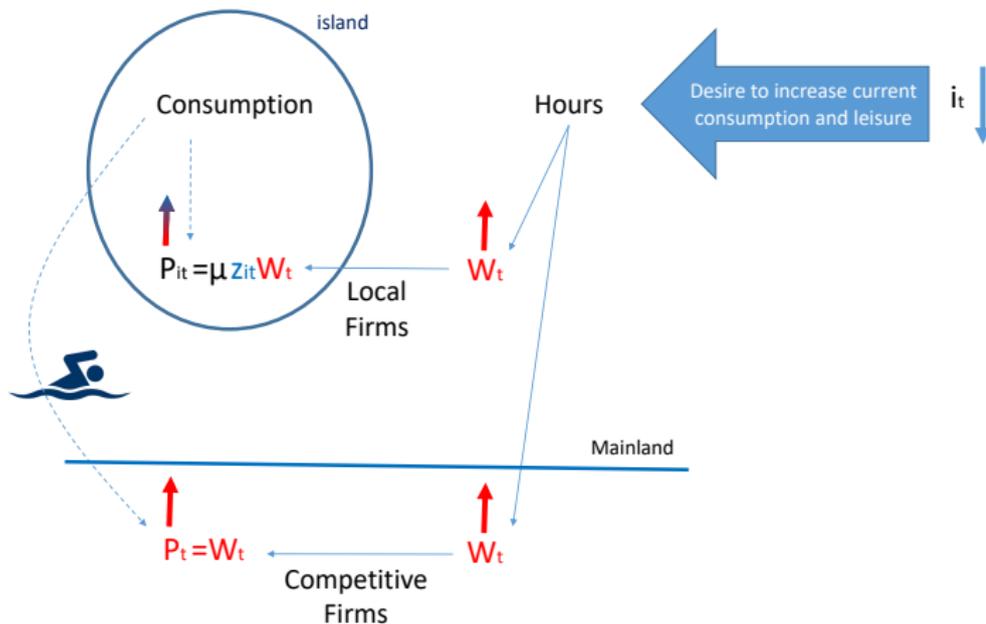


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Two types of firms: local (high markup) and competitive (low/no-markup)

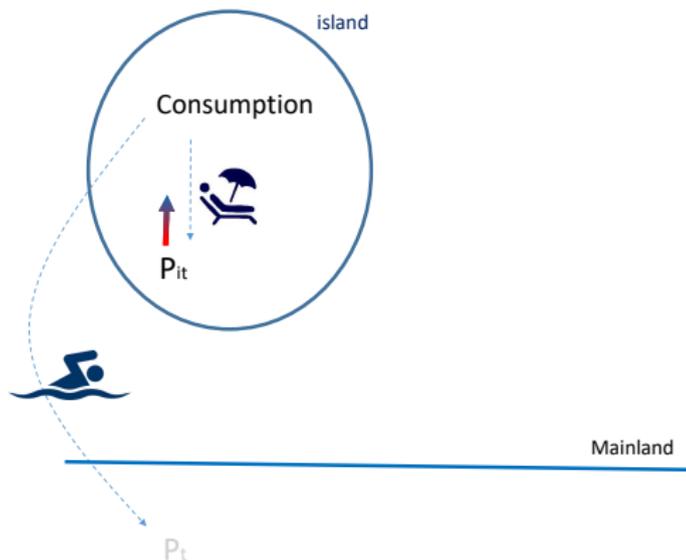
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**Real rigidity:** Shopping costs individual-specific effort.

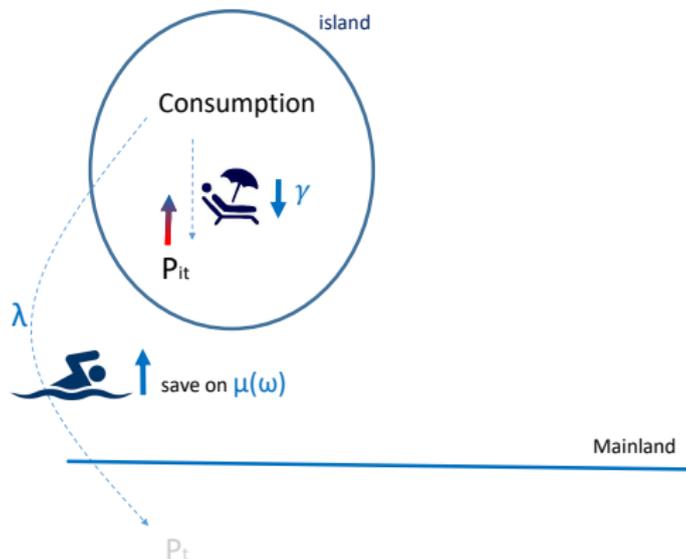
## CARTOON SUMMARY



Two types of firms: local (high markup) and competitive (low/no-markup)

**Info rigidity:** Shopping choice conditional to local prices only.

## CARTOON SUMMARY



Conditional to an aggregate nominal shock:

- ▶ swimmers:  $\uparrow$  consumption due to  $\downarrow$  markup  $\Rightarrow$  **effective price rigidity**

# OUTLINE

- ▶ Model
- ▶ Demand-Driven Business Cycles
  - ▶ Aggregate Counter-Cyclical Markup
  - ▶ Firm-level Markups: A-cyclical but Endogenous to Hs' Uncertainty
  - ▶ Welfare
- ▶ Empirics: a test of inflation-driven shopping reallocation
- ▶ Extensions
  - ▶ Households' vs Local Firms' Uncertainty
  - ▶ Targeted Communication
  - ▶ Local Varieties
  - ▶ Firms' Common Uncertainty (sticky prices)

## DEMAND-DRIVEN BUSINESS CYCLE FLUCTUATIONS

Agg. consumption (switchers + non-switchers) of agents type  $j$ :

$$C_{jt} - C^* = \underbrace{\mathcal{N}(p_{jt})}_{\substack{\text{mass of local buyers} \\ \downarrow \text{ with } P_t \\ \text{less positive}}} \times \underbrace{(\mathcal{C}(p_{jt}) - C^*)}_{\substack{\text{local consumption loss} \\ \downarrow \text{ with } P_t \\ \text{more negative}}}$$

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In particular:

$$\ln C_t - \ln \bar{C} \approx [\lambda \mu(\omega)^\gamma - \lambda - \gamma] \bar{\alpha} (1 - \omega) \pi_t,$$

with  $\bar{\alpha}$  denoting the steady state share of expenditure in the local market, and  $\bar{C}$  steady state aggregate consumption.

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- This is why firms **must** be bad compared to Hs in the NK framework.

## AGGREGATE COUNTERCYCLICAL MARKUP

The effective average markup:

$$\mathcal{M}_t^{eff} \equiv \frac{P_t^{eff}}{W_t} = 1 + \alpha_t (\mu - 1),$$

where  $\alpha_t$  denotes the market share of local sellers and is given by

$$\alpha_t = \frac{\bar{\mathcal{N}} \bar{\mathcal{C}} e^{-(\lambda+\gamma)(1-\omega)\pi_t}}{1 - \bar{\mathcal{N}} e^{-\lambda(1-\omega)\pi_t} + \bar{\mathcal{N}} \bar{\mathcal{C}} e^{-(\lambda+\gamma)(1-\omega)\pi_t}}.$$

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$\alpha_t$  co-moves negatively with  $\pi_t$ , in fact:

$$\ln \alpha_t - \ln \bar{\alpha} \approx -[\bar{\alpha} \lambda \mu^\gamma + (1 - \bar{\alpha})(\gamma + \lambda)] (1 - \omega) \pi_t$$

where  $\bar{\alpha}$  is the value of  $\alpha_t$  at  $\pi_t = 0$ .

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**The aggregate markup is countercyclical.**

Let us now turn to how  $\omega$  shapes  $\mu$

## LEARNING FROM PRICES AND LOCAL MARKUPS

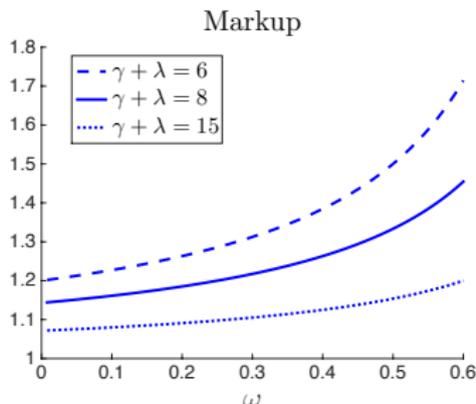
→  $\omega$  denotes the elasticity of Hs' inflation exp. w.r.t. local prices.

$$E[\pi_t | \Omega_t^s] = \frac{\sigma_z^{-2}}{\underbrace{\sigma_\pi^{-2} + \sigma_z^{-2}}_{\omega}} (\ln p_{jt} - E[\ln p_{jt} | \Omega_{t-1}]).$$

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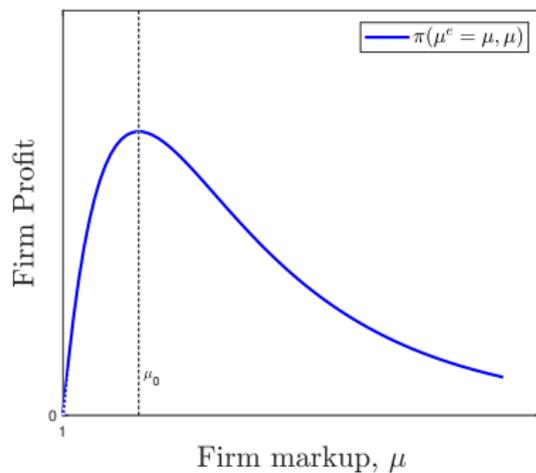
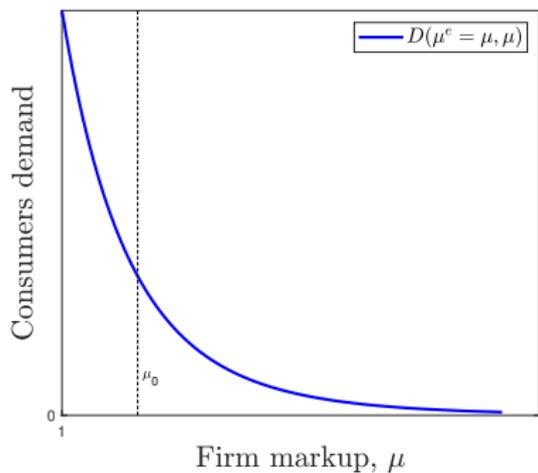
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The optimal markup set by firm  $j$  is endogenous but **time/state-invariant**:

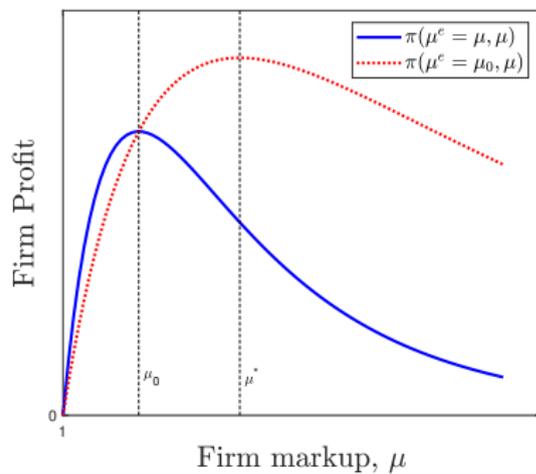
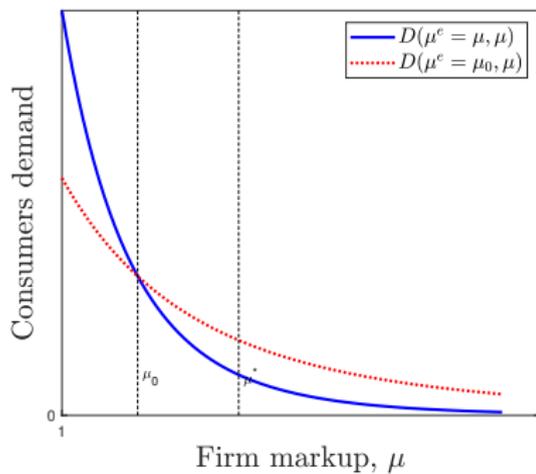
$$\mu(\omega) = \begin{cases} \frac{(\gamma+\lambda)(1-\omega)}{(\gamma+\lambda)(1-\omega)-1} & \text{with } \omega < \frac{\gamma+\lambda-1}{\gamma+\lambda}, \\ +\infty & \text{with } \omega \geq \frac{\gamma+\lambda-1}{\gamma+\lambda}, \end{cases}$$

## CONFUSION AND DISCRETION IN PRICING



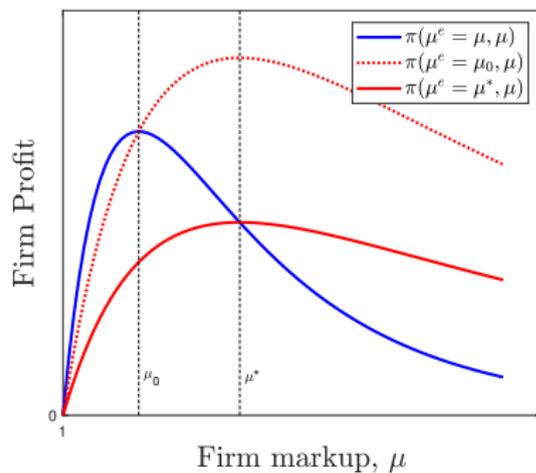
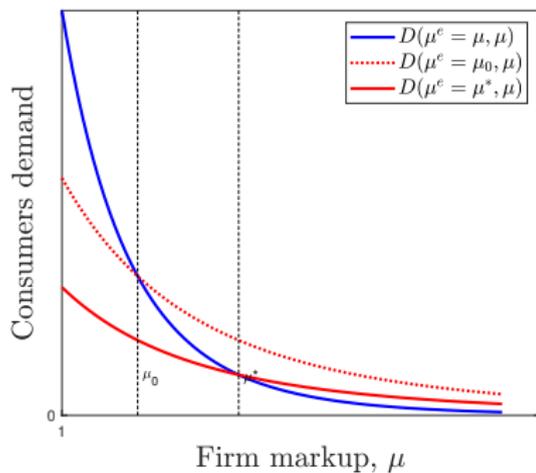
Without any signaling power we have the standard firm problem.

# CONFUSION AND DISCRETION IN PRICING



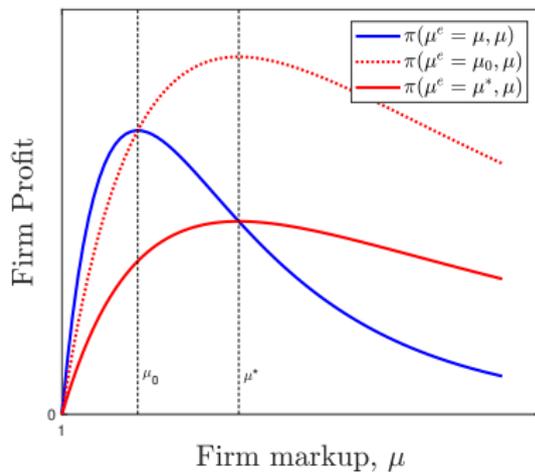
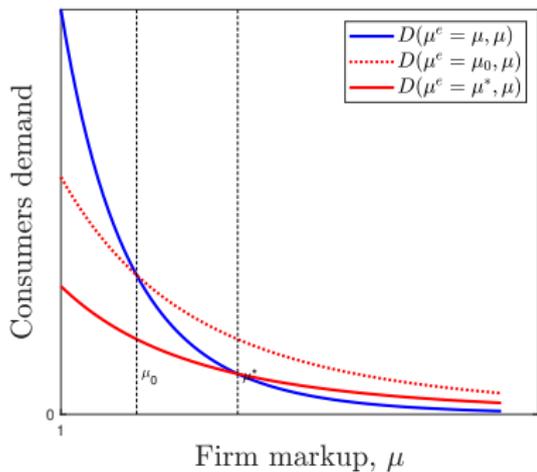
Signalling power induces firms to increase their markups.

# CONFUSION AND DISCRETION IN PRICING



However, as Hs anticipate  $\mu^*$ , their demand shifts down!

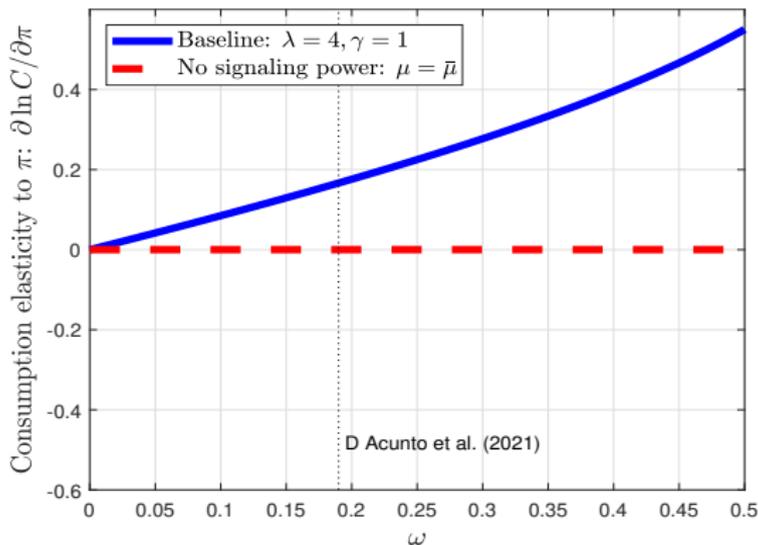
# CONFUSION AND DISCRETION IN PRICING



Signaling power creates a commitment problem, hurting firms' profits.

# DEMAND-DRIVEN BUSINESS CYCLE FLUCTUATIONS

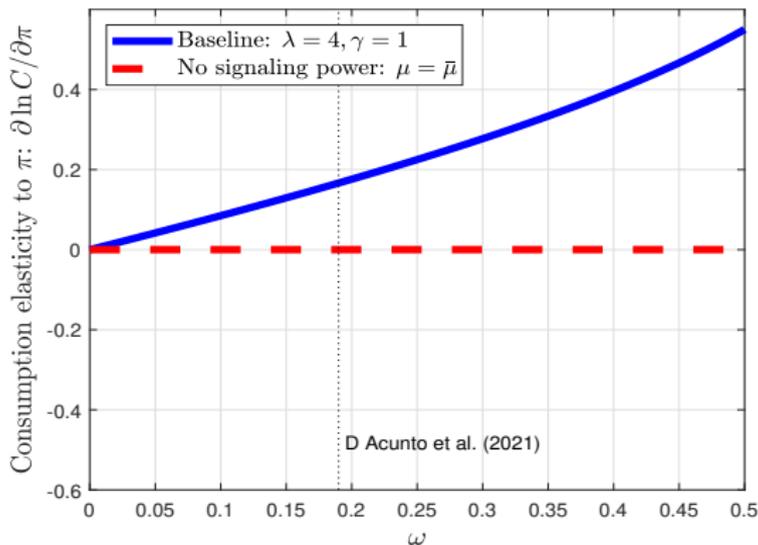
FIGURE: The consumption-inflation comovement



dashed :  $(\gamma = 1, \omega = 0) \Rightarrow [\lambda \mu(\omega)^\gamma - \lambda - \gamma] = 0$

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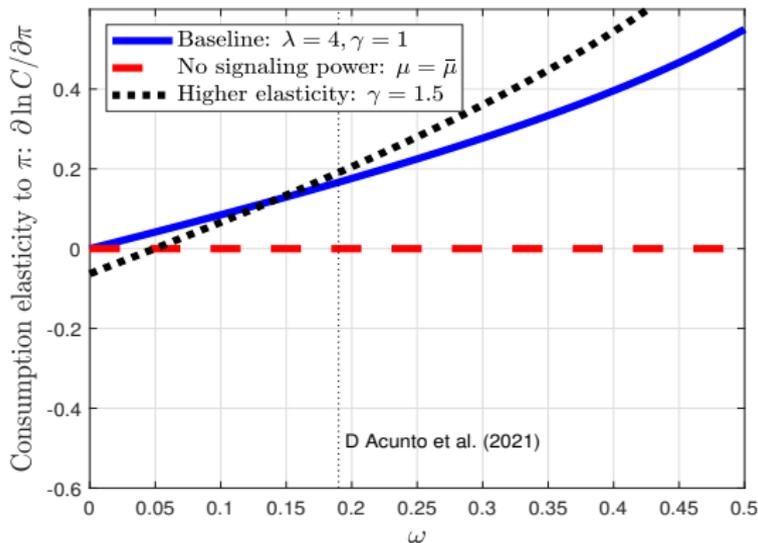
FIGURE: The consumption-inflation comovement



**solid** :  $(\gamma = 1, \omega > 0) \Rightarrow [\lambda \mu(\omega)^\gamma - \lambda - \gamma] > 0$

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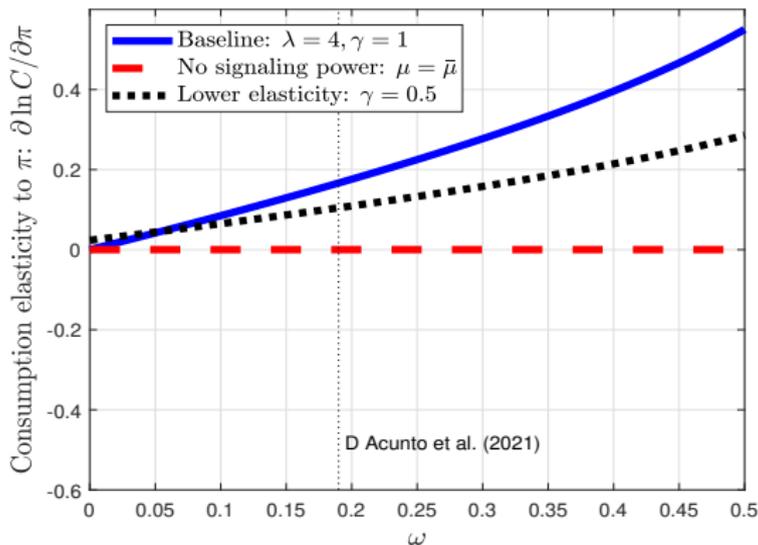
FIGURE: The consumption-inflation comovement



$$\text{dotted : } (\gamma = 1.5, \omega > \bar{\omega}) \Rightarrow [\lambda \mu(\omega)^\gamma - \lambda - \gamma] > 0$$

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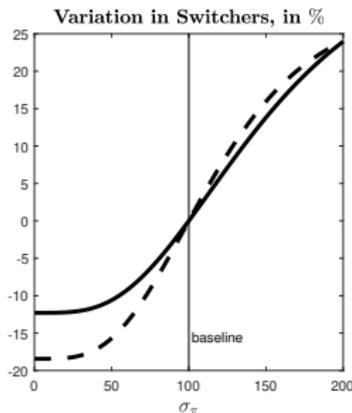
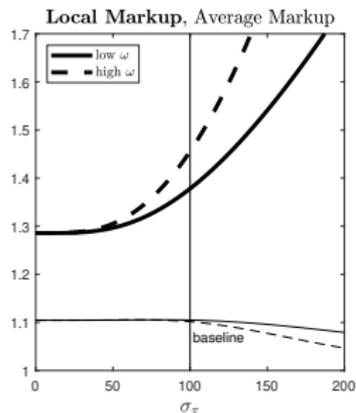
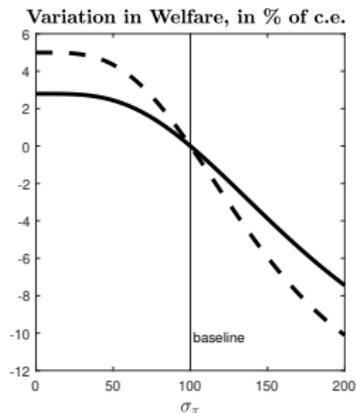
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$$\text{dotted : } (\gamma = 0.5, \omega \geq 0) \Rightarrow [\lambda \mu(\omega)^\gamma - \lambda - \gamma] > 0$$

# WELFARE AND POLICIES OF UNCERTAINTY REDUCTION

$$\uparrow \text{inflation volatility} \Rightarrow \uparrow \omega = \frac{1}{1 + \frac{\sigma_{\pi}^2}{\sigma_{\mu}^2}} \Rightarrow \uparrow \mu$$



Note: The figure shows how welfare varies with  $\sigma_{\pi}^2$ . The vertical dotted line corresponds to the baseline value of  $\sigma_{\pi} = 0.35\%$ . Welfare is calculated in equivalent consumption growth with respect to baseline consumption. We fixed  $\gamma = .5, \lambda = 4$  and  $\varphi = 1$ . Calibration is such that at baseline,  $\rho = 0.1$  and  $\omega = 0.29$  for the dashed line and  $\omega = 0.19$  for the solid line.

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## EMPIRICS: EFFECTIVE VS POSTED INFLATION

- **effective inflation:**  $\pi_t^{eff}$  effective per unit price
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  - ▶ covariance with inflation: 0 in NK (fig NK);
  - ▶  $\neq 0$  in our model

$$\pi_t^{eff} - \pi_t^{pos} \approx -\bar{\alpha}(\mu - 1) \underbrace{[\bar{\alpha} \lambda \mu^\gamma + (1 - \bar{\alpha})(\lambda + \gamma)]}_{\log \alpha_t - \log \bar{\alpha}} (1 - \omega) \pi_t.$$

- ▶  $< 0$  if households less informed than firms

## DATA

- ▶ Information Resources Inc. (“IRI”), weekly price and quantity information 2001-2011 on items (UPC  $\times$  Store  $\times$  Market).
- ▶ Method: Coibion et al. (AER15), Gagnon et al. (AER17)
- ▶ **Effective** vs **Posted** price and inflation for UPC  $j$  in market  $m$ :

$$p_{mj,t}^{eff} = \frac{\sum_{s \in S_m} TR_{mjs,t}}{\sum_{s \in S_m} TQ_{mjs,t}} \implies \pi_{mj,t}^{eff} = \ln p_{mj,t}^{eff} - \ln p_{mj,t-1}^{eff}$$

$$p_{mj,t}^{pos} = \sum_{s \in S_m} \bar{w}_{msj} \frac{TR_{mjs,t}}{TQ_{mjs,t}} \implies \pi_{mj,t}^{pos} = \ln p_{mj,t}^{pos} - \ln p_{mj,t-1}^{pos}$$

- ▶ Average over  $j$  within category  $c$  and market  $m$ , monthly:

$$\pi_{mc,t}^{eff} = \frac{1}{J} \sum_{j \in c} \pi_{mj,t}^{eff} \quad \text{and} \quad \pi_{mc,t}^{pos} = \frac{1}{J} \sum_{j \in c} \pi_{mj,t}^{pos}$$

## MONETARY SHOCK

- ▶ Romer-Romer (2004) updated by Wieland-Yang (2019), 2001-2007, monthly
- ▶ Instrument  $\pi_{mc,t}^{pos}$  with MP shock  $\epsilon_t$
- ▶ First stage:

$$\pi_{mc,t}^{pos} = \beta \epsilon_t + h_{mc} + error_{mc,t}$$

- ▶ Significant effect on posted price inflation:  $\hat{\beta} = -1.82^{***}$

## EFFECTIVE VS POSTED INFLATION

We estimate the following relationship:

$$\pi_{mc,t}^{eff} - \pi_{mc,t}^{pos} = \rho \pi_{m,t} + \iota u_{m,t} + f_t + h_{mc} + error_{mc,t},$$

where  $\pi_{m,t} = (1/N_c) \times \sum_{c \in S_m} \pi_{mc,t}^{pos}$ .

	(1)	(2)	(3)	(4)	(5)
Inflation, $\pi_{m,t}$	-0.44*** (0.043)	-0.45*** (0.044)	-0.42*** (0.032)	-0.42*** (0.034)	-1.93*** (0.425)
Unemployment, $u_{m,t}$		-0.15*** (0.04)		-0.013 (0.04)	-1.25*** (0.27)
Stratum F.E.	Yes	Yes	Yes	Yes	Yes
Month F.E.	Yes	Yes	Yes	Yes	No
IV regression	No	No	No	No	Yes
Weighted regression	No	No	Yes	Yes	No

Robust prediction: when inflation increases (decreases), effective paid inflation increases (decreases) less than posted inflation  $\implies$  **sticky effective inflation**

## EFFECTIVE VS POSTED INFLATION

Run regression for effective inflation and sales growth,  $s_{mc,t}$ :

$$x_{mc,t} = \rho \pi_{mc,t}^{pos} + \iota u_{m,t} + h_{mc} + error_{mc,t}$$

	(1)	(2)	(3)	(4)
	$\pi_{mc,t}^{eff}$	$\pi_{mc,t}^{eff}$	$\pi_{mc,t}^{eff}$	$s_{mc,t}$
Inflation, $\pi_{m,t}^{pos}$	<b>0.79***</b>	<b>0.36**</b>	<b>0.34**</b>	3.59***
	(0.015)	(0.18)	(0.19)	(0.75)
Unemployment, $u_{m,t}$			<b>-0.55***</b>	
			(0.11)	
Robust S.E.	Yes	Yes	Yes	Yes
Stratum F.E.	Yes	Yes	Yes	Yes
Month F.E.	Yes	No	No	No
IV regression	No	Yes	Yes	Yes

- ▶ Incomplete pass-through of posted price to effective price inflation
- ▶ Meaningful expenditure reallocation across retailers

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## AN EXTENDED INFO STRUCTURE

★ Local firms' uncertainty about inflation innovations:

$$E[\pi_t | \Omega_{jt}^f] = \delta (\pi_t + u_{jt})$$

so that  $p_{jt} = \mu e^{E[\ln W_t | \Omega_{jt}^f] + \frac{1}{2} \nu - \ln z_{jt}}$ ;

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★ Households' expectations are expressed as

$$E[\pi_t | \Omega_{jt}^s] = \rho (\pi_t + \nu_{jt}) + \omega (\ln p_{jt} - E[\ln p_{jt} | \Omega_{t-1}]),$$

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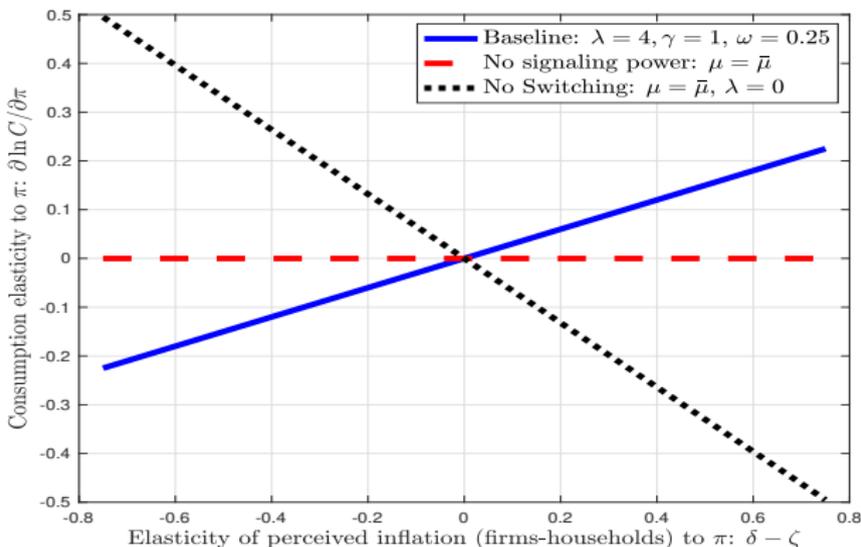
★ Households perceived real local price is

$$\int_0^1 \ln p_{jt} - E[\ln P_t | \Omega_{jt}^s] dj = \ln \mu + \underbrace{(\delta - \zeta)}_{\text{info gap}} \pi_t.$$

where  $\zeta \equiv \omega\delta + \rho$ .

## INFORMATION GAP

FIGURE: The consumption-inflation comovement and the information gap



Note: We set  $\sigma_z / \sigma_\pi$  so that  $\omega = 0.25$  and  $\kappa$  so that  $\bar{\alpha} = 0.66$  in all simulations. We report the elasticity of consumption to an inflation shock at different combinations of  $\lambda$  and  $\gamma$ , and for different values of  $\delta - \zeta$  on the horizontal axis obtained either by varying  $\delta$  and/or  $\rho$ . In the baseline specification we use  $\lambda = 4$  and  $\gamma = 1$  (solid blue line). The red dashed line plots a counterfactual where  $\mu = (\lambda + \gamma) / (\lambda + \gamma - 1)$ . The black dotted line also sets  $\lambda = 0$ .

## EXTENSION WITH FIRMS' COMMON UNCERTAINTY

A firms – distant and local – receive a common signal:

$$\vartheta_t : \pi + u_t$$

with  $u_t \sim N(0, \sigma_u^2)$ . Thus  $P_t = E[W_t | \Omega_t^f]$ .

Aggregate consumption is now expressed as:

$$\begin{aligned} \ln C_t - \ln \bar{C} &\approx \bar{\alpha} (\lambda \mu^\gamma - \gamma - \lambda) ((\delta - \zeta) \pi_t + \delta(1 - \omega) u_t) \\ &\quad + \bar{\alpha} \left( \lambda (\mu^\gamma - 1) (\mu^\lambda - 1) + \gamma \right) \hat{\rho} (1 - \delta) \pi_t \\ &\quad + \bar{\alpha} \mu^\gamma \mu^\lambda (1 - \mu^{-\lambda}) \gamma \tilde{\rho} ((1 - \delta) \pi_t - \delta u_t). \end{aligned}$$

with  $\hat{\rho}$  being the loading of Hs' signal on the expected difference  $P_t - W_t$ .

- First line: main case + (exp.) noise.
- Second line: positive effect of Hs info about real wage on switching
- Third line: positive effect of Hs info on intensive margins + (contr.) noise.

## LOCAL VARIETIES

$c_{ijt}$  is an aggregate over the  $X$  varieties,

$$c_{ijt} = X \left( \frac{1}{X} \sum_{x=0}^X c_{xijt}^{\frac{\epsilon-1}{\epsilon}} \right)^{\frac{\epsilon}{\epsilon-1}}$$

with  $\epsilon > 1$  being the elasticity of substitution across varieties, whose price is:

$$p_{jt} = \left( \frac{1}{X} \sum_{n=0}^N p_{xjt}^{1-\epsilon} \right)^{\frac{1}{1-\epsilon}}.$$

Each local firm  $x \in \{1, 2, \dots, X\}$  chooses the price  $p_{xjt}$  that maximizes profits

$$p_{xjt} = \operatorname{argmax}_p \mathcal{N}_{jt}(p) \mathcal{D}_{xjt}(p) \left( \frac{p}{W_t} - z_{jt} \right)$$

with  $\mathcal{D}_{xjt}(p) = \int c_{xijt} di = c_{ijt} \left( \frac{p}{p_{jt}} \right)^{-\epsilon} di$ .

In equilibrium,  $\mu = \frac{\xi}{\xi-1}$  where

$$\xi = \left( 1 - \frac{1}{X} \right) \epsilon + \frac{1}{X} (\gamma + \lambda)(1 - \omega).$$

# Conclusions

## CONCLUSIONS

We have built on the idea that inflation provides incentives to more aggressive shopping.

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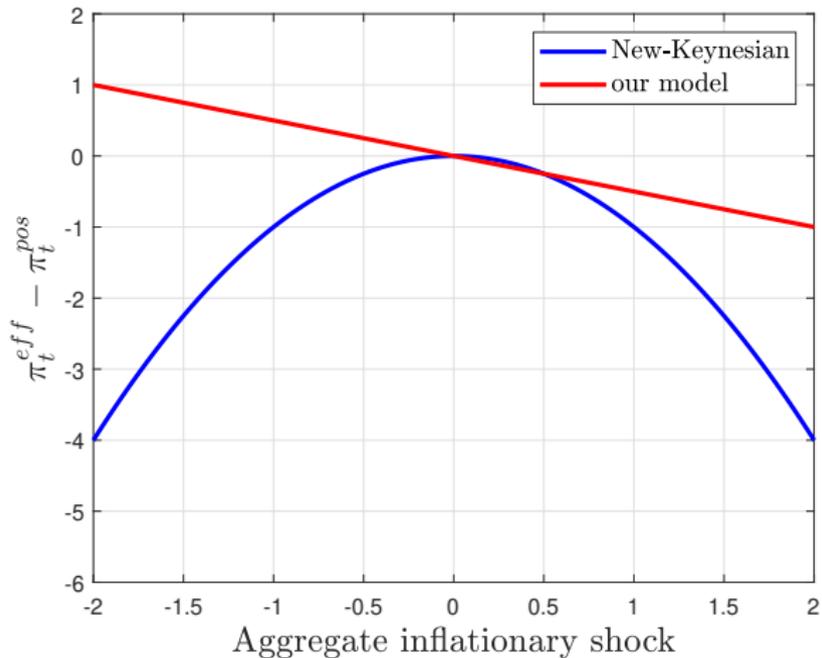
**Demand-driven Countercyclical Aggregate Markup +**

**...but fixed firm-level markups!**

Thanks

# Appendix

### R.3. THE RESPONSE OF THE INFLATION GAP



With deflationary shocks consumers reallocate towards local markets to save shopping effort.

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## MICRO-EVIDENCE ON MARKUP CYCLICALITY

### ▶ **Macro models call for countercyclical markups**

Bils, Klenow and Malin (2018): “Thus, countercyclical price markups deserve a central place in business-cycle research.”

### ▶ **Micro evidence seems pointing towards a-cyclical markups**

Anderson, Rebelo and Wong (2018): “markups are relatively stable over time and mildly procyclical”;

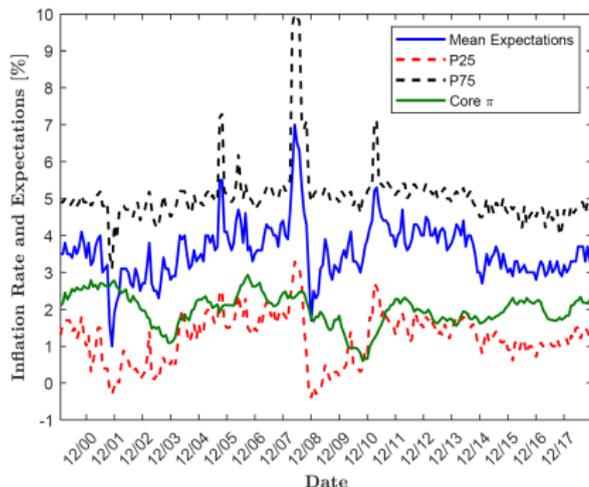
Burstein, Carvalho and Grassi (2020): “exploiting different reduced-form measures of markup cyclicality, two researchers may arrive at opposing conclusions even within a single dataset.”

**Q: How to reconcile Macro call with Micro evidence?**

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# HOW WELL HOUSEHOLDS PREDICT INFLATION?

Figure 5: Inflation Expectations and Realized Core Inflation over Time



Notes. This figure plots average inflation expectations over time from the Michigan Survey of Consumers together with the 25<sup>th</sup> and 75<sup>th</sup> percentiles as well as the realized core inflation rate for a sample period from January 2000 until December 2018.

Source: D'Acunto et al. (2019)

## THREE FACTS ON EXPECTATIONS AND SHOPPING

### ▶ **Shopping prices influence expectations**

Expectation Survey Bank of England: first source of information

D'Acunto, Malmendier, Ospina and Weber (2021): CPI Household  $\sim 0.2$ ; CPI Frequency  $\sim 0.3$

### ▶ **Arbitrage across shops: valuable but limited**

Menzio and Kaplan (2016): visiting one additional store:  $\sim -0.6\%$  Indiv-CPI; shopping concentrated: 2.3 shops visited on average per quarter

### ▶ **Expected<sup>2</sup> inflation less dispersed than experienced<sup>1</sup>**

<sup>1</sup> Michigan Survey: inter. range 3.8%

<sup>2</sup> Kaplan and Schulhofer-Wohl (2017): inter. range 7.3%

**Q: how to reconcile the frictional household (micro) with output-inflation comovement (macro)?**

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## MODEL PREDICTIONS

$$\ln C_t - \ln \bar{C} \propto (\lambda \mu^\gamma - \gamma - \lambda) (1 - \omega) \pi_t.$$

- ▶ Fix  $\lambda = 4$ ,  $\gamma = 1$ ,  $\bar{\alpha} = 0.66$  from the literature.
- ▶ Use regression to pin down info gap  $1 - \omega$ .
- ▶ How large is the response of consumption to inflation as we vary  $\mu$ ?

